## GAUTENG PROVINCE

EDUCATION
REPUBLIC OF SOUTH AFRICA

## GAUTENG DEPARTMENT OF EDUCATION

## PROVINCIAL EXAMINATION

## 2016

GRADE 11


## MEMORANDUM

11 pages

| MEMORANDUM | Mathematics P2 |
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## GAUTENG DEPARTMENT OF EDUCATION

## PROVINCIAL EXAMINATION

## MATHEMATICS

(Second Paper)

## INFORMATION:

A - Accuracy
C.A. - Continued Accuracy

S $\quad-\quad$ Statement
R - Reason
S and R - Statement and Reason

|  | QUESTION 1 | MARKS : 16 |
| :---: | :---: | :---: |
| 1.1 | $\begin{aligned} \mathrm{KT} & =\sqrt{\left(x_{2}-x_{1}\right)^{2}+\left(y_{2}-y_{1}\right)^{2}} \\ & =\sqrt{(-5-1)^{2}+(1-6)^{2}} \\ & =\sqrt{61} \end{aligned}$ | $\checkmark$ Distance formula <br> $\checkmark$ subst. in corr. formula <br> $\checkmark$ answer <br> [2/3 if answer not in surd form] |
| 1.2 | $\begin{aligned} m_{K P} & =\frac{y_{2}-y_{1}}{x_{2}-x_{1}} \\ & =-\frac{1}{4} \end{aligned}$ $\begin{aligned} \left(y-y_{1}\right) & =m\left(x-x_{1}\right) \\ (y-1) & =-\frac{1}{4}(x-(-5)) \\ y & =-\frac{1}{4} x-\frac{1}{4} \end{aligned}$ <br> OR $\begin{aligned} m_{K P} & =\frac{y_{2}-y_{1}}{x_{2}-x_{1}} \\ & =-\frac{1}{4} \end{aligned}$ $\begin{aligned} (y-(-2)) & =-\frac{1}{4}(x-7) \\ y & =-\frac{1}{4} x-\frac{1}{4} \end{aligned}$ | $\checkmark$ answer $m_{K P}$ <br> $\checkmark$ subst. $(-5 ; 1)$ into str. line eq. <br> $\checkmark$ answer (C.A) <br> OR <br> $\checkmark$ answer $m_{K P}$ <br> $\checkmark$ subst. (7;-2) into str. line eq. <br> $\checkmark$ answer (C.A) |
| 1.3 | $\begin{aligned} & m_{K T}=\frac{6-1}{1-(-5)} \\ &=\frac{5}{6} \\ &(y-6)=\frac{5}{6}(x-1) \\ & y=\frac{5}{6} x+5 \frac{1}{6} \\ & \mathrm{~A}\left(0 ; 5 \frac{1}{6}\right) \\ & \mathrm{B}\left(0 ;-\frac{1}{4}\right) \\ & \mathrm{AB}=5 \frac{1}{6}+\frac{1}{4} \\ &=5 \frac{5}{12} \quad \text { OR } 5,42 \quad \text { OR } \frac{65}{12} \end{aligned}$ | $\checkmark$ answer $m_{K T}$ (A) <br> $\checkmark$ eq. of Line KT. (A) OR y-int of line KT. <br> $\checkmark$ add of $y$ co-ord. of A and B <br> $\checkmark$ answer (A) |


| 1.4 | $\begin{aligned} & \tan \beta=m_{K T} \\ & \tan \beta=\frac{5}{6} \\ & \beta=39,81^{\circ} \\ & m_{P T}=-\frac{4}{3} \\ & \tan \alpha=-\frac{4}{3} \\ & \begin{array}{c} \alpha=180^{\circ}-53,13^{\circ} \\ =126,87^{\circ} \\ \theta=\alpha-\beta \ldots . . . . . e x t . \quad \text { of } \Delta \\ =126,87^{\circ}-39,81^{\circ} \\ =87,06^{\circ} \end{array} \end{aligned}$ <br> ANY other valid solution | $\begin{align*} & \checkmark \tan \beta=\frac{5}{6} \\ & \checkmark \beta=39,81^{\circ} \\ & \checkmark \\ & \tan \alpha=-\frac{4}{3} \\ & \checkmark \alpha=126,87^{\circ} \\ & \checkmark 126,87^{\circ}-39,81^{\circ} \\ & \checkmark \text { answer } \\ & \text { (PENALISE once for rounding } \\ & \text { off, either } \alpha \text { or } \beta \text { ) } \tag{6} \end{align*}$ |
| :---: | :---: | :---: |
|  | QUESTION 2 | MARKS : 14 |
| 2.1 | Let M ( $x ; y$ ) $\begin{aligned} & O M^{2}=M B^{2} \ldots \ldots \text { radii) } \\ & (0-x)^{2}+(0-y)^{2} \\ & =(8-x)^{2}+(0-y)^{2} \\ & x^{2}+y^{2} \\ & =64-16 x+x^{2}+y^{2} \\ & x \end{aligned}$ | $\checkmark O M^{2}=M B^{2}$ <br> $\checkmark$ corr. Subst. in dist. formula <br> $\checkmark$ simplification (C.A) <br> $\checkmark$ answer <br> Answer only 0 |
| 2.2 | $\begin{gathered} \mathrm{A}(x ; y) \\ x=0 \\ \frac{0+y}{2}=2 \\ y=4 \\ \mathrm{~A}(0 ; 4) \end{gathered}$ | $\checkmark$ subst. in midpt. formula <br> $\checkmark y=0$ <br> $\checkmark$ co-ord. of A <br> [2/3 if not in co-ordinate form] |
| 2.3 | $m_{A B}=-\frac{1}{2}$ <br> Eq. of line OK: $\begin{aligned} y-y_{1} & =m\left(x-x_{1}\right) \\ y-0 & =-\frac{1}{2}(x-0) \\ y & =-\frac{1}{2} x \end{aligned}$ | $\checkmark m_{A B}$ <br> $\checkmark$ corr. subst. in str. line formula <br> $\checkmark$ answer (C.A) |


| 2.4 | $\begin{align*} & \text { Let } \mathrm{T}(x ; y) \\ & m_{A T}=\frac{4-y}{-x} \\ & \frac{4-y}{-x} \times-\frac{1}{2}=-1 \ldots \ldots . \perp \text { lines } \\ & y=2 x+4 \ldots . . . . . . . . . . . . . .(1) \tag{1} \end{align*}$ <br> Eq. of line OK $\begin{gather*} y=-\frac{1}{2} x  \tag{2}\\ 2 x+4=-\frac{1}{2} x \\ x=-\frac{8}{5} \tag{4} \end{gather*}$ <br> Any other valid method | $\begin{aligned} & \checkmark \frac{4-y}{-x} \times-\frac{1}{2}=-1 \\ & \checkmark y=2 x+4 \end{aligned}$ <br> $\checkmark$ equating (1) and (2) <br> $\checkmark$ answer (C.A) |
| :---: | :---: | :---: |
|  | QUESTION 3 | MARKS 28 |
| 3.1 | $\begin{aligned} 13 \sin \alpha & =-5 \\ \sin \alpha & =-\frac{5}{13} \end{aligned}$  $\begin{aligned} x & =-\sqrt{13^{2}-(-5)^{2}} \\ & =-12 \end{aligned}$ <br> $3 \cos \alpha$ $\begin{aligned} & =3\left(-\frac{12}{13}\right) \\ & =-\frac{36}{13} \end{aligned}$ | $\checkmark \sin \alpha=-\frac{5}{13}$ <br> $\checkmark$ cartesian plane with terminal arm in 3 rd quad. $\checkmark x=-12$ <br> $\checkmark$ subst. $\cos \alpha=-\frac{12}{13}$ |
|  |  |  |


| 3.2.1 | $\begin{aligned} & \frac{\sin \left(\theta-180^{\circ}\right) \cdot \tan \left(360^{\circ}-\theta\right) \cdot \sin \left(90^{\circ}-\theta\right)}{\cos ^{2}\left(\theta+180^{\circ}\right)} \\ & =\frac{-\sin \theta \times-\tan \theta \times \cos \theta}{\cos ^{2} \theta} \\ & =\frac{-\sin \theta \times-\frac{\sin \theta}{\cos \theta} \times \cos \theta}{\cos ^{2} \theta} \\ & =\frac{\sin ^{2} \theta}{\cos ^{2} \theta} \\ & =\tan ^{2} \theta \end{aligned}$ | $\checkmark-\sin \theta ; \quad \checkmark-\tan \theta ; \checkmark \cos \theta$; <br> $\checkmark \cos ^{2} \theta$ $\checkmark-\tan \theta=-\frac{\sin \theta}{\cos \theta}$ <br> $\checkmark \frac{\sin ^{2} \theta}{\cos ^{2} \theta}$ or $\tan ^{2} \theta$ |
| :---: | :---: | :---: |
| 3.2.2 | $\begin{align*} & \frac{\sin 210^{\circ} \cdot \cos 400^{\circ}}{\sin \left(-50^{\circ}\right) \times \cos 120^{\circ}}  \tag{6}\\ & =\frac{\sin \left(180^{\circ}+30^{\circ}\right) \times \cos \left(360^{\circ}+40^{\circ}\right)}{-\sin 50^{\circ} \times \cos \left(180^{\circ}-60^{\circ}\right)} \\ & =\frac{-\sin 30^{\circ} \times \cos 40^{\circ}}{-\cos 40^{\circ} \times-\cos 60^{\circ}} \\ & =-1 \end{align*}$ | $\begin{align*} & \checkmark-\sin 50^{\circ} \\ & \checkmark-\sin 30^{\circ} ; \\ & \checkmark \cos 40^{\circ} ; \\ & \checkmark-\cos 40^{\circ} \text { or } \cos 40^{\circ}=\sin 50^{\circ} \\ & \checkmark-\cos 60^{\circ} \\ & \checkmark \text { answer } \tag{6} \end{align*}$ |
| 3.3 | $\begin{aligned} & (4 \theta-8) \sin 30^{\circ}=\theta^{3}-8 \\ & (4 \theta-8) \sin 30^{\circ}=(\theta-2)\left(\theta^{2}+2 \theta+4\right) \\ & (4 \theta-8) \sin 30^{\circ}=(\theta-2)(2) \\ & \sin 30^{\circ}=\frac{(\theta-2)(2)}{(4 \theta-8)} \\ & \quad=\frac{(\theta-2)(2)}{4(\theta-2)} \\ & \quad=\frac{1}{2} \end{aligned}$ | $\checkmark$ factorization <br> $\checkmark$ factorization of denominator <br> $\checkmark$ answer |


|  | $\begin{aligned} \tan 240^{\circ} & =\tan \left(180^{\circ}+60^{\circ}\right) \\ & =\tan 60^{\circ} \\ & =\sqrt{3} \end{aligned}$ | $\checkmark \tan 60^{\circ}$ <br> $\checkmark$ answer <br> Full marks if $\tan 60^{\circ}=\sqrt{3}$ or Show sketch to determine sol. Answer only max 1 mark(surd form) |
| :---: | :---: | :---: |
| 3.4.1 | $\text { L.H.S: } \begin{align*} & \frac{1}{\tan x}(\sin \alpha \tan \alpha+\cos \alpha) \\ &=\sin \alpha+\frac{\cos \alpha}{\tan \alpha} \\ &=\sin \alpha+\frac{\frac{\cos \alpha}{\frac{\sin \alpha}{\cos \alpha}}}{} \\ &=\sin \alpha+\frac{\cos ^{2} \alpha}{\sin \alpha} \\ &= \frac{\sin ^{2} \alpha+\cos ^{2} \alpha}{\sin \alpha}  \tag{4}\\ &=\frac{1}{\sin \alpha}=\text { R.H.S } \end{align*}$ <br> Any other valid method | $\begin{aligned} & \checkmark \sin \alpha+\frac{\cos \alpha}{\tan \alpha} \\ & \checkmark \text { subst. } \tan \alpha=\frac{\sin \alpha}{\cos \alpha} \\ & \checkmark \frac{\cos ^{2} \alpha}{\sin \alpha} \\ & \checkmark \frac{\sin ^{2} \alpha+\cos ^{2} \alpha}{\sin \alpha} \end{aligned}$ |
| 3.4.2 | $\alpha=\left\{0^{\circ} ; 90^{\circ} ; 180 ; 270^{\circ} ; 360^{\circ}\right\}$ | $\begin{align*} & \checkmark 0^{\circ} ; 180^{\circ} ; 360^{\circ} \\ & \checkmark 90^{\circ} ; 270^{\circ} \tag{2} \end{align*}$ |


|  | QUESTION 4 | MARKS 12 |
| :---: | :---: | :---: |
| 4.1 | $180^{\circ}$ | $\checkmark$ answer |
| 4.2 | $y \in[-1 ; 1]$ <br> OR $-1 \leq y \leq 1, y \in \mathrm{R}$ | $\checkmark-1 ; 1$ <br> $\checkmark$ corr. brackets <br> OR $\checkmark-1 ; 1$ <br> $\checkmark$ corr. inequalities |
| 4.3 | $\begin{aligned} & \theta=40^{\circ} \\ & a=2 \end{aligned}$ | $\begin{aligned} & \checkmark 40^{\circ} \\ & \checkmark 2 \end{aligned}$ |
| 4.4 | $\mathrm{g}\left(180^{\circ}\right)=-0,77$ | $\checkmark$ answer (C.A) |
| 4.5.1 | $\begin{aligned} & f(x)-g(x)>0 \\ & f(x)>g(x) \\ & -180^{\circ} \leq x<-103,3^{\circ} \text { OR } \\ & {\left[-180^{\circ} ;-103,3^{\circ}\right)} \end{aligned}$ | $\checkmark-180^{\circ} ;-103,3^{\circ}$ <br> $\checkmark$ corr. inequality OR <br> corr. bracket <br> OR <br> $\left(16,7^{\circ} ; 130^{\circ}\right)$ or $\left(136,7^{\circ} ; 180^{\circ}\right]$ |
|  |  | (2) |
| 4.5.2 | $\begin{aligned} & g(x) \cdot f(x) \geq 0 \\ & {\left[-130^{\circ} ;-90^{\circ}\right] \text { OR }} \\ & -130^{\circ} \leq x \leq-90^{\circ} \end{aligned}$ | $\checkmark\left[-130^{\circ} ;-90^{\circ}\right]$ <br> $\checkmark$ corr brackets OR corr. inequalities $\left[0^{\circ} ; 50^{\circ}\right] \text { or }\left[90^{\circ} ; 180\right]$ |
| 4.6 | $\begin{aligned} & 3^{\cos \left(90^{3}-2 x\right)} \\ & =3^{\sin 2 x} \\ & =3^{-1} \\ & \text { OR } \\ & =\frac{1}{3} \end{aligned}$ | $\sqrt{ } 3^{\sin 2 x}$ <br> $\checkmark$ answer <br> (2) |


|  | QUESTION 5 | MARKS 8 |  |
| :---: | :---: | :---: | :---: |
| 5.1 | is perpendicular to the chord | $\checkmark$ answer |  |
| 5.2.1 | $\begin{aligned} \mathrm{AD} & =\sqrt{A B^{2}+B D^{2}} \ldots \text { th. of pyth. } \\ & =\sqrt{24^{2}+16^{2}} \\ & =28,84 \mathrm{~cm} \end{aligned}$ | $\checkmark$ Subst. <br> $\checkmark$ answer | (1) |
|  |  |  | (2) |
| 5.2.2 | $\mathrm{OD}=x+16$ | $\checkmark$ answer |  |
| 5.2.3 | $\begin{aligned} & \mathrm{OC}^{2}=\mathrm{BC}^{2}+\mathrm{OB}^{2} \ldots \ldots . . \text { th. of pyth } \\ & O D^{2}=24^{2}+x^{2} \\ & (x+16)^{2}=24^{2}+x^{2} \\ & \\ & \begin{array}{c} x^{2}+32 x+256=576+x^{2} \\ 32 x=320 \\ x=10 \end{array} \end{aligned}$ | $\mathrm{OC}^{2}=\mathrm{BC}^{2}+\mathrm{OB}^{2}$ <br> $\mathrm{OC}=\mathrm{OD} . . .$. radii $\begin{aligned} & \checkmark(x+16)^{2} \\ & \checkmark 24^{2}+x^{2} \end{aligned}$ <br> $\checkmark$ simplification <br> $\checkmark$ answer |  |
|  | QUESTION 6 | MARKS 8 |  |
| 6.1 | $\mathrm{PT}=\frac{1}{2} \mathrm{KT} . . . . .$. line from centre $\perp$ to ch. | $\begin{aligned} & \checkmark \mathrm{S} \\ & \checkmark \mathrm{R} \end{aligned}$ |  |
| 6.2 | $\begin{aligned} & K C^{2}=P C^{2}+K P^{2} \ldots . . . \text { th. of pyth. } \\ & \text { but } K P^{2}=O K^{2}-O P^{2} \ldots . . \text { th. of pyth. } \\ & K C^{2}=P C^{2}+O K^{2}-O P^{2} \\ & \quad \text { but } O K=O C \ldots . . \text { radii } \\ & \quad=P C^{2}+O C^{2}-(O C-P C)^{2} \backslash \\ & \quad=P C^{2}+O C^{2}-\left(O C^{2}-2 O C . P C+P C^{2}\right) \\ & \quad=2(O C . P C) \\ & \quad=2(x+y)(y) \\ & \quad=2 x y+2 y^{2} \end{aligned}$ | $\checkmark$ S <br> $\checkmark K P^{2}=O K^{2}-O P^{2}$ <br> $\checkmark$ subst. $\mathrm{OK}=\mathrm{OC}$ <br> $\checkmark$ subst. $\mathrm{OP}=\mathrm{OC}-\mathrm{PC}$ <br> $\checkmark$ simplification <br> $\checkmark$ subst. for OC and PC |  |
|  |  |  | (6) |



| 7.5 | $\begin{aligned} & \hat{T}=45^{\circ} \\ & \widehat{T}=\widehat{Q}=45^{\circ} \\ & \therefore \mathrm{TR} / / \mathrm{PQ} . . . . . . \text { alt. } \mathrm{Ls}= \\ & \\ & \\ & \\ & \mathrm{TRP}=45^{\circ} \\ & \mathrm{TRP}=\widehat{\mathrm{P}}=45^{\circ} \\ & \therefore \mathrm{TR} / / \mathrm{PQ} . . . . . . \text { alt. }\llcorner\mathrm{s}= \end{aligned}$ | $\begin{aligned} & \checkmark \hat{T}=45^{\circ} \\ & \checkmark \mathrm{R} \end{aligned}$ <br> OR <br> $\checkmark T \hat{R} P=\widehat{P}$ <br> $\checkmark$ R |  |
| :---: | :---: | :---: | :---: |

